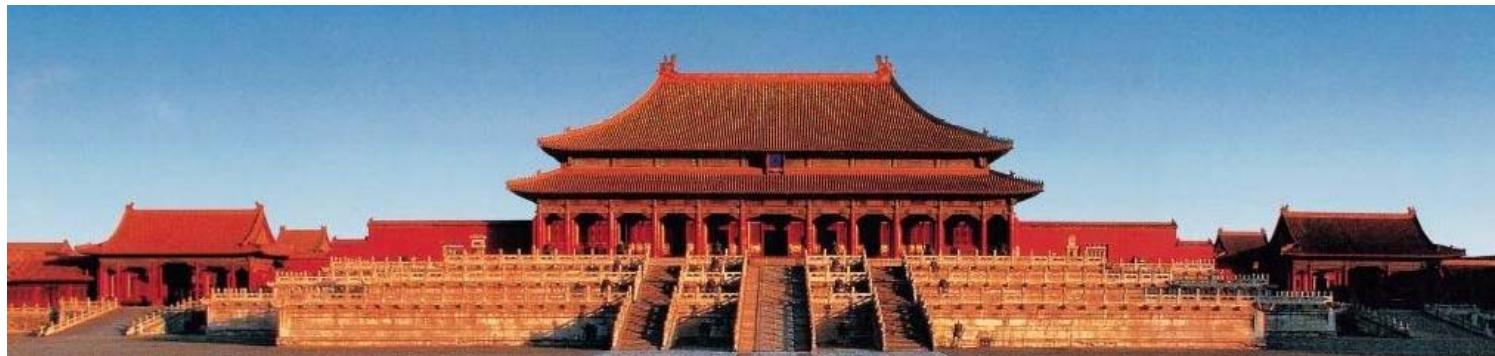


# Heavy quark spectroscopy and accurate prediction of b-baryon masses



**QNP09, IHEP, Beijing**

Marek Karliner

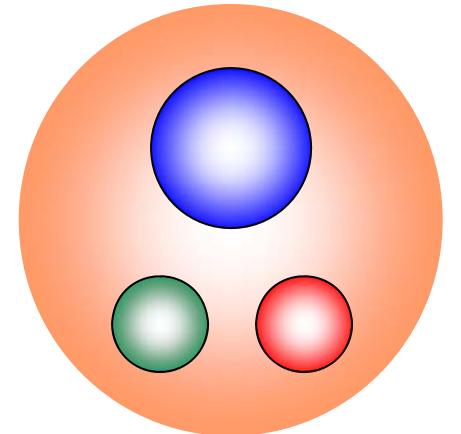
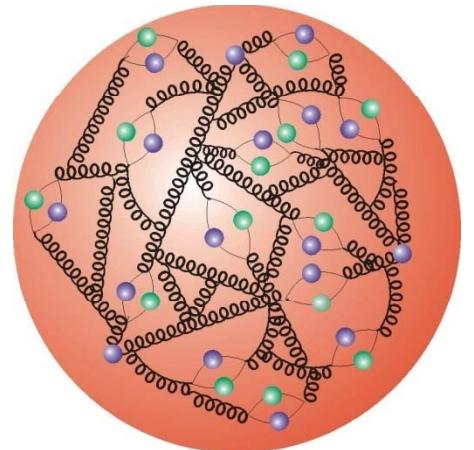
in collaboration with B. Keren-Zur, H.J. Lipkin and J. Rosner

# Constituent Quark Models (CQM)

- QCD describes hadrons as valence quarks in a sea of gluons and q-qbar pairs.
- at low E,  $\chi$ SB
- → quark constituent mass
- hadron can be considered as a bound state of constituent quarks.
- Sakharov-Zeldovich formula:

$$M = \sum_i m_i$$

- the binding & kinetic energies “swallowed” by the constituent quarks masses.



# Color Hyperfine (HF) interaction

- 1st correction – color hyperfine (chromo-magnetic) interaction

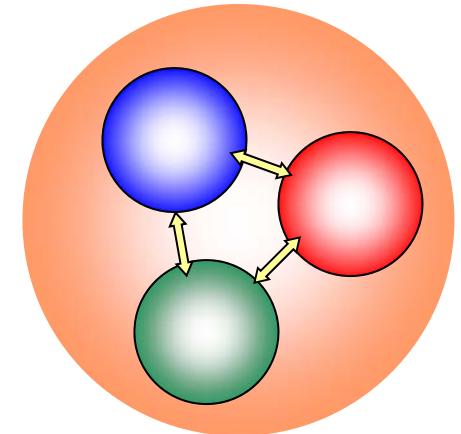
$$M = \sum_i m_i + \sum_{i < j} V^{HF}_{ij}$$

$$V^{HF(QCD)}_{ij} = v_0 (\vec{\lambda}_i \cdot \vec{\lambda}_j) \frac{\vec{\sigma}_i \cdot \vec{\sigma}_j}{m_i m_j} \langle \psi | \delta(r_i - r_j) | \psi \rangle$$

- A contact interaction
- Analogous to the EM hyperfine interaction – a product of the magnetic moments.

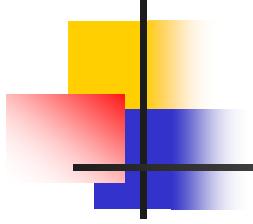
$$V^{HF(em)}_{ij} \propto \vec{\mu}_i \cdot \vec{\mu}_j = e^2 \frac{\vec{\sigma}_i \cdot \vec{\sigma}_j}{m_i m_j}$$

- In QCD, SU(3) generators take the place of the electric charge.



# Constituent Quark Model: *caveat emptor*

- a low energy limit, phenomenological model
- still awaiting derivation from QCD
- far from providing a full explanation of the hadronic spectrum, but it provides excellent predictions for mass splittings and magnetic moments
- assumptions:
  - HF interaction considered as a perturbation
  - → does not change the wave function
  - same masses for quarks inside mesons and baryons.
  - no 3-body effects.

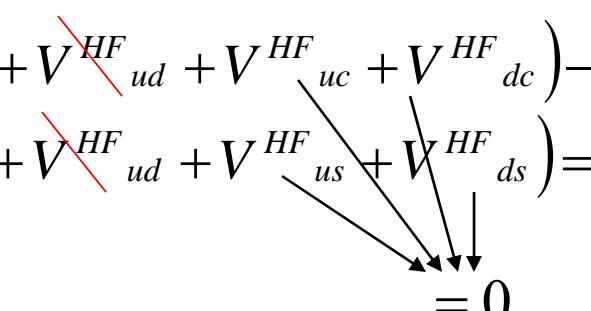


# constituent quark masses

- example I:  
quark mass differences from baryon mass differences:

$$\begin{aligned} M_{\Lambda_c} - M_{\Lambda} &= \\ &= \left( \cancel{m_u} + \cancel{m_d} + m_c + V^{HF}_{ud} + V^{HF}_{uc} + V^{HF}_{dc} \right) - \\ &\quad - \left( \cancel{m_u} + \cancel{m_d} + m_s + V^{HF}_{ud} + V^{HF}_{us} + V^{HF}_{ds} \right) = \\ &= m_c - m_s \end{aligned}$$

$= 0$



# constituent quark masses

- example II:

$$\begin{aligned} M_{K^*} - M_K &= v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_{\bar{s}})}{m_u m_s} [(\vec{\sigma}_u \cdot \vec{\sigma}_{\bar{s}})_{K^*} - (\vec{\sigma}_u \cdot \vec{\sigma}_{\bar{s}})_K] \langle \psi | \delta(r) | \psi \rangle \\ &= 4v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_{\bar{s}})}{m_u m_s} \langle \psi | \delta(r) | \psi \rangle \end{aligned}$$

- extracting quark masses ratio:

$$\frac{M_{K^*} - M_K}{M_{D^*} - M_D} = \frac{4v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_{\bar{s}})}{m_u m_s} \langle \psi | \delta(r) | \psi \rangle}{4v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_{\bar{c}})}{m_u m_c} \langle \psi | \delta(r) | \psi \rangle} \approx \frac{m_c}{m_s}$$

TABLE I - Quark mass differences from baryons and mesons

quark mass difference is the same  
in mesons and baryons

$$\langle m_i - m_j \rangle_{dBar} \approx \langle m_i - m_j \rangle_{dMes}$$

but depends on the spectator quark

**→ challenge to npQCD**

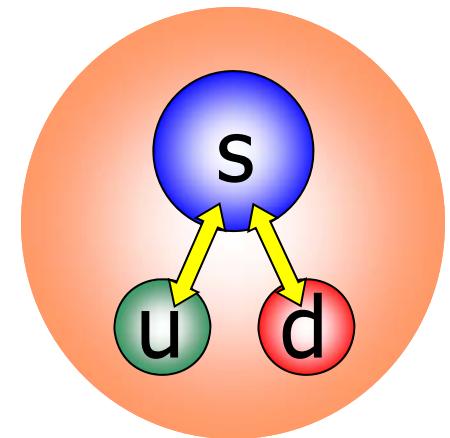
MK & Lipkin, hep-ph/0307243

observable	baryons		mesons				$\Delta m_{Bar}$	MeV	
			$J = 1$	$J = 0$	$\mathcal{P}_i$	$\mathcal{P}_j$			
	$B_i$	$B_j$	$\mathcal{V}_i$	$\mathcal{V}_j$	$K^*$	$\rho$	$K$	$\pi$	$\Delta m_{Mes}$
$\langle m_s - m_u \rangle_d$	$\Lambda$	$sud$	$uud$	$s\bar{d}$	$u\bar{d}$	$s\bar{d}$	$u\bar{d}$	177	179
		$N$		$K^*$	$\rho$	$K$	$\pi$		
$\langle m_s - m_u \rangle_c$				$c\bar{s}$	$c\bar{u}$	$c\bar{s}$	$c\bar{u}$		103
				$D_s^*$	$D_s^*$	$D_s$	$D_s$		
$\langle m_s - m_u \rangle_b$				$b\bar{s}$	$b\bar{u}$	$b\bar{s}$	$b\bar{u}$		91
				$B_s^*$	$B_s^*$	$B_s$	$B_s$		
$\langle m_c - m_u \rangle_d$	$\Lambda_c$	$cud$	$und$	$c\bar{d}$	$u\bar{d}$	$c\bar{d}$	$u\bar{d}$	1346	1360
		$N$		$D^*$	$\rho$	$D$	$\pi$		
$\langle m_c - m_u \rangle_c$				$c\bar{c}$	$u\bar{c}$	$c\bar{c}$	$u\bar{c}$		1095
				$\psi$	$D^*$	$\eta_c$	$D$		
$\langle m_c - m_s \rangle_d$	$\Lambda_c$	$cud$	$sud$	$c\bar{d}$	$s\bar{d}$	$c\bar{d}$	$s\bar{d}$	1169	1180
		$\Lambda$		$D^*$	$K^*$	$D$	$K$		
$\langle m_c - m_s \rangle_c$				$c\bar{c}$	$s\bar{c}$	$c\bar{c}$	$s\bar{c}$		991
				$\psi$	$D_s^*$	$\eta_c$	$D_s$		
$\langle m_b - m_u \rangle_d$	$\Lambda_b$	$bud$	$uud$	$b\bar{d}$	$u\bar{d}$	$b\bar{d}$	$u\bar{d}$	4685	4700
		$N$		$B^*$	$\rho$	$B$	$\pi$		
$\langle m_b - m_u \rangle_s$				$b\bar{s}$	$u\bar{s}$	$b\bar{s}$	$u\bar{s}$		4613
				$B_s^*$	$K^*$	$B_s$	$K$		
$\langle m_b - m_s \rangle_d$	$\Lambda_b$	$bud$	$sud$	$b\bar{d}$	$s\bar{d}$	$b\bar{d}$	$s\bar{d}$	4508	4521
		$\Lambda$		$B^*$	$K^*$	$B$	$K$		
$\langle m_b - m_c \rangle_d$	$\Lambda_b$	$bud$	$sud$	$b\bar{d}$	$c\bar{d}$	$b\bar{d}$	$c\bar{d}$	3339	3341
		$\Lambda_c$		$B^*$	$D^*$	$B$	$D$		
$\langle m_b - m_c \rangle_s$				$b\bar{s}$	$c\bar{s}$	$b\bar{s}$	$c\bar{s}$		3328
				$B_s^*$	$D_s^*$	$B_s$	$D_s$		7

# color hyperfine splitting in baryons

- The  $\Sigma$  (uds) baryon HF splitting:

- $\Sigma^*$ : total spin 3/2 -  
u and d at relative spin – 1
  - $\Sigma$  : isospin – 1
    - Symmetric under exchange of u and d
    - u and d at relative spin – 1



$$(\vec{\sigma}_u \cdot \vec{\sigma}_d)_{\Sigma^*} = (\vec{\sigma}_u \cdot \vec{\sigma}_d)_{\Sigma}$$

- the ‘ud’ pair does not contribute to the HF splitting

$$M_{\Sigma^*} - M_{\Sigma} = 6v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_s)}{m_u m_s} \langle \psi | \delta(r_{ij}) | \psi \rangle$$

## Quark mass ratio from HF splittings in mesons and baryons

$$\left(\frac{m_c}{m_s}\right)_{Bar} = \frac{M_{\Sigma^*} - M_\Sigma}{M_{\Sigma_c^*} - M_{\Sigma_c}} = 2.84 = \left(\frac{m_c}{m_s}\right)_{Mes} = \frac{M_{K^*} - M_K}{M_{D^*} - M_D} = 2.81$$

$$\left(\frac{m_c}{m_u}\right)_{Bar} = \frac{M_\Delta - M_p}{M_{\Sigma_c^*} - M_{\Sigma_c}} = 4.36 = \left(\frac{m_c}{m_u}\right)_{Mes} = \frac{M_\rho - M_\pi}{M_{D^*} - M_D} = 4.46$$

New type of mass relations with more heavy flavors

$$\left( \frac{\frac{1}{m_u^2} - \frac{1}{m_u m_c}}{\frac{1}{m_u^2} - \frac{1}{m_u m_s}} \right)_{Bar} = \frac{M_{\Sigma_c} - M_{\Lambda_c}}{M_\Sigma - M_\Lambda} = 2.16 \approx \left( \frac{\frac{1}{m_u^2} - \frac{1}{m_u m_c}}{\frac{1}{m_u^2} - \frac{1}{m_u m_s}} \right)_{Mes} = \frac{(M_\rho - M_\pi) - (M_{D^*} - M_D)}{(M_\rho - M_\pi) - (M_{K^*} - M_K)} = 2.10$$

Similar relation for bottom baryons  
→ prediction for  $\Sigma_b$  mass

$$\frac{M_{\Sigma_b} - M_{\Lambda_b}}{M_\Sigma - M_\Lambda} = \frac{(M_\rho - M_\pi) - (M_{B^*} - M_B)}{(M_\rho - M_\pi) - (M_{K^*} - M_K)} = 2.51$$

→  $M_{\Sigma_b} - M_{\Lambda_b} = 194 \text{ MeV}$

(MK & Lipkin, hep-ph/0307243)

# Observation of New Heavy Baryon $\Sigma_b$ and $\Sigma_b^*$

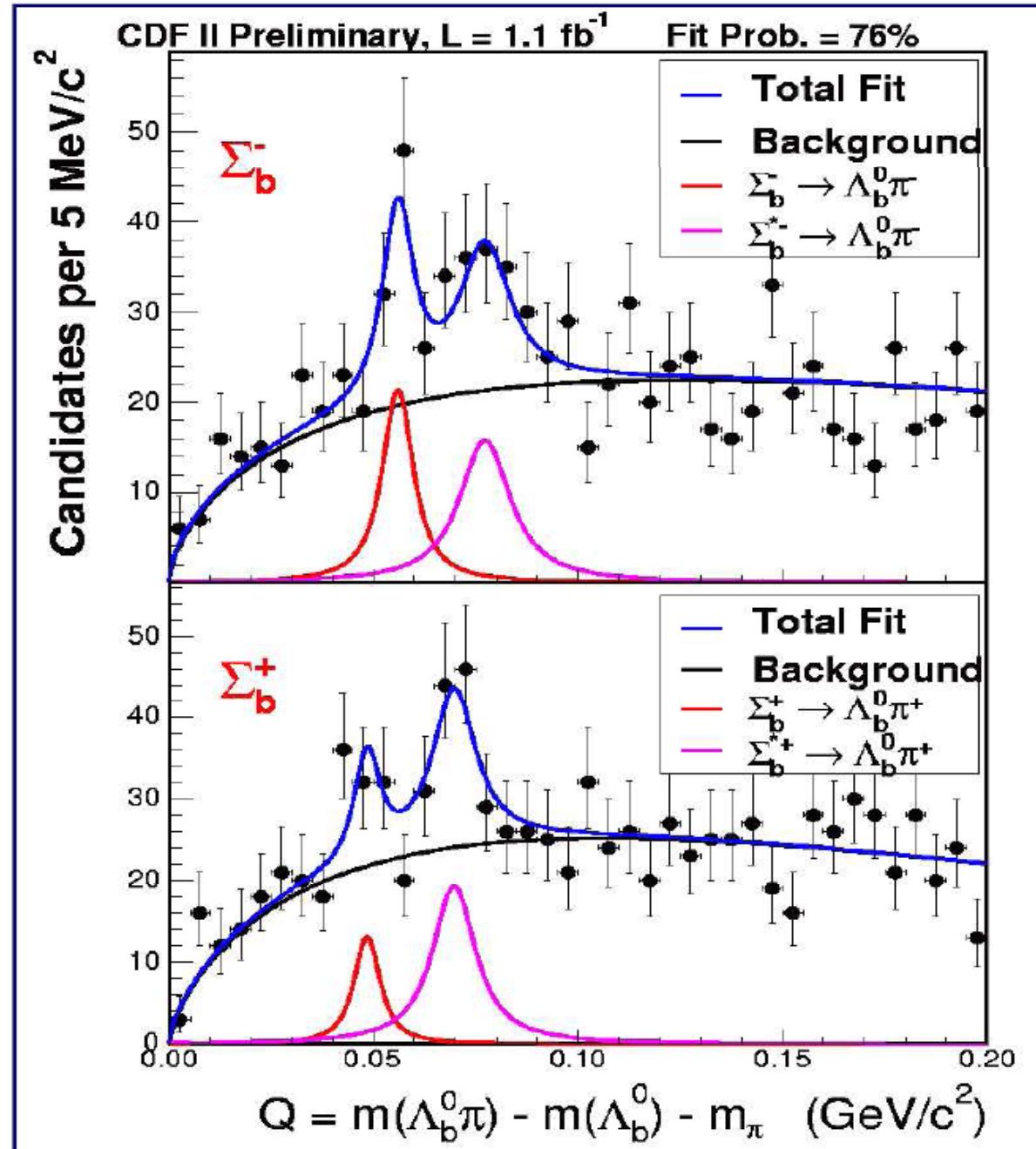
*This web page summarizes the results of the search for new heavy baryons  $\Sigma_b$  and  $\Sigma_b^*$  based upon  $1fb^{-1}$  of data. The results have been approved as of September 21, 2006.*

*The ratio of likelihoods of the null-hypothesis ( no  $\Sigma_b^{(*)\pm}$  signal) and the hypothesis of four  $\Sigma_b^{(*)\pm}$  states is  $2.6 \times 10^{-19}$ . Using the fully reconstructed decay mode*

$$\Sigma_b^{(*)\pm} \rightarrow \Lambda_b^0 \pi^\pm; \quad \Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-; \quad \Lambda_c^+ \rightarrow p K^- \pi^+$$

*we measure:*

- $m(\Sigma_b^+) = 5808^{+2.0}_{-2.3} (\text{stat.}) \pm 1.7 (\text{syst.}) \text{ MeV}/c^2$
- $m(\Sigma_b^-) = 5816^{+1.0}_{-1.0} (\text{stat.}) \pm 1.7 (\text{syst.}) \text{ MeV}/c^2$
- $m(\Sigma_b^{*+}) = 5829^{+1.6}_{-1.8} (\text{stat.}) \pm 1.7 (\text{syst.}) \text{ MeV}/c^2$
- $m(\Sigma_b^{*-}) = 5837^{+2.1}_{-1.9} (\text{stat.}) \pm 1.7 (\text{syst.}) \text{ MeV}/c^2$

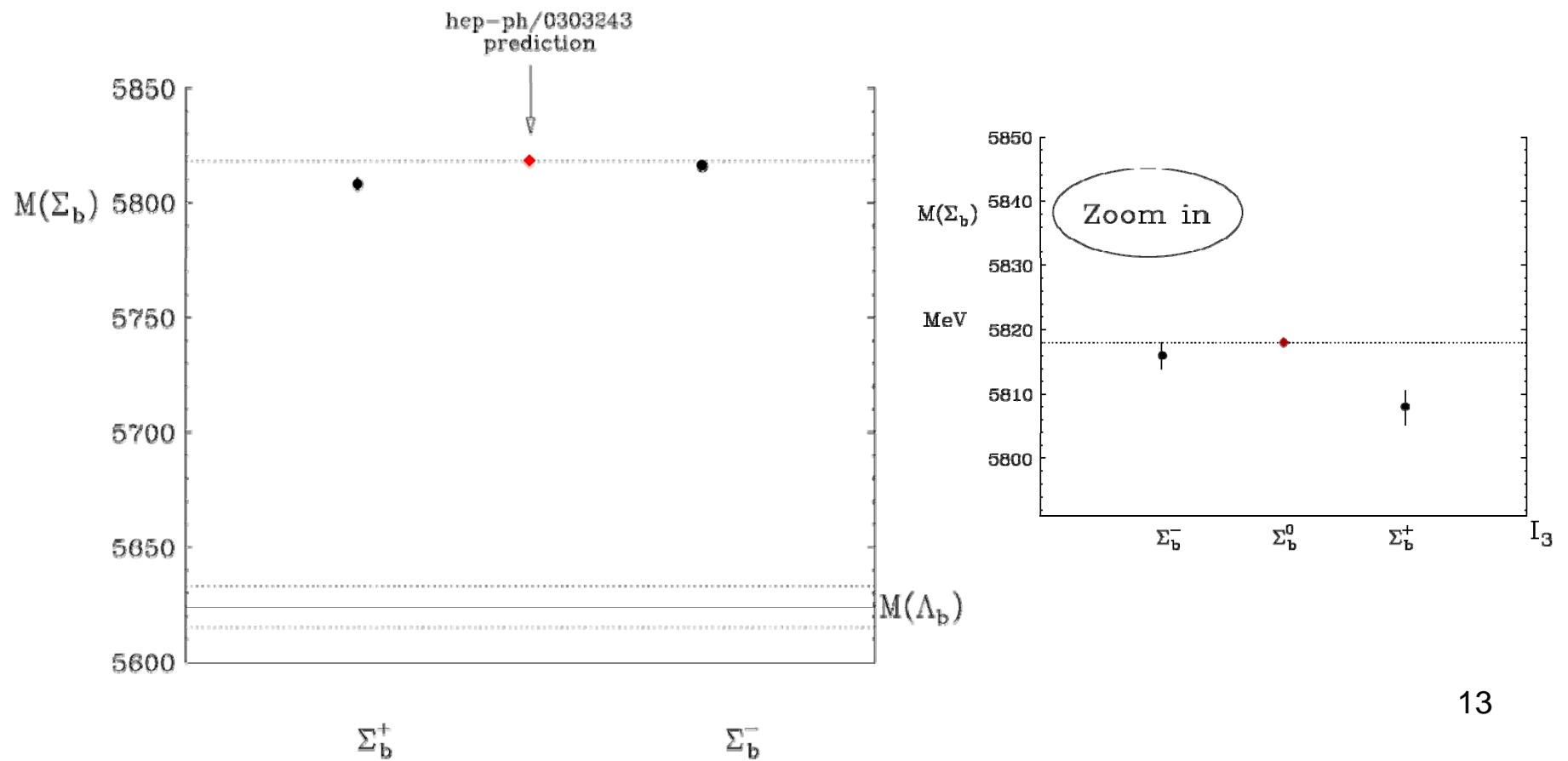


CDF obtained the masses of the  $\Sigma_b^-$  and  $\Sigma_b^+$  from the decay  $\Sigma_b \rightarrow \Lambda_b + \pi$  by measuring the corresponding mass differences |

$$M(\Sigma_b^-) - M(\Lambda_b) = 195.5^{+1.0}_{-1.0} (\text{stat.}) \pm 0.1 (\text{syst.}) \text{ MeV}$$

$$M(\Sigma_b^+) - M(\Lambda_b) = 188.0^{+2.0}_{-2.3} (\text{stat.}) \pm 0.1 (\text{syst.}) \text{ MeV}$$

with isospin-averaged mass difference  $M(\Sigma_b) - M(\Lambda_b) = \boxed{192 \text{ MeV.}}$



can rederive without assuming  $\text{HF} \sim 1/m_q$

a weaker assumption of same flavor dependence suffices

$$\frac{V_{hyp}(q_i \bar{q}_j)}{V_{hyp}(q_i \bar{q}_k)} = \frac{V_{hyp}(q_i q_j)}{V_{hyp}(q_i q_k)}$$

$$\frac{M_{\Sigma_b} - M_{\Lambda_b}}{(M_\rho - M_\pi) - (M_{B^*} - M_B)} = \frac{M_{\Sigma_c} - M_{\Lambda_c}}{(M_\rho - M_\pi) - (M_{D^*} - M_D)} = \frac{M_{\Sigma} - M_{\Lambda}}{(M_\rho - M_\pi) - (M_{K^*} - M_K)}$$

0.32                       $\approx$                       0.33                       $\approx$                       0.325

also prediction for spin splitting between  $\Sigma_b^*$  and  $\Sigma_b$

$$M(\Sigma_b^*) - M(\Sigma_b) = \frac{M(B^*) - M(B)}{M(K^*) - M(K)} \cdot [M(\Sigma^*) - M(\Sigma)] = 22 \text{ MeV}$$

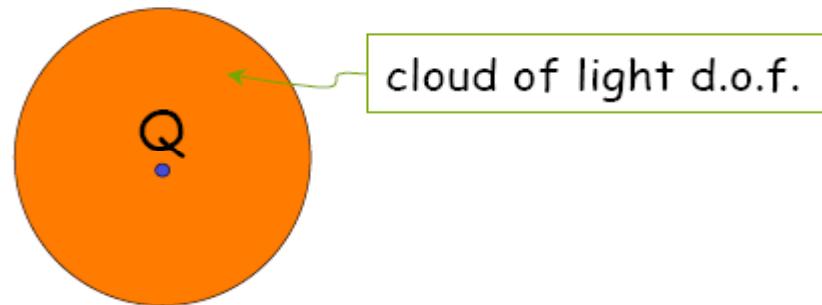
to be compared with 21 MeV from the isospin-average of CDF measurements

$$M(\Sigma_b^{*-}) = 5837_{-1.9}^{+2.1} \text{ (stat.)} \pm 1.7 \text{ (syst.) MeV}$$

$$M(\Sigma_b^{*+}) = 5829_{-1.8}^{+1.6} \text{ (stat.)} \pm 1.7 \text{ (syst.) MeV}$$

# Effective meson-baryon supersymmetry

- meson:  $Q \bar{q}$  baryon:  $Q q\bar{q}$
- in both cases: valence quark coupled to light quark “brown muck” color antitriplet, either a light antiquark ( $S=1/2$ ) or a light diquark ( $S=0, S=1$ )



- Effective supersymmetry:  $T_{LS}^S |\mathcal{M}(\bar{q}Q_i)\rangle \equiv |\mathcal{B}([q\bar{q}]_S Q_i)\rangle$
- $m(\mathcal{B}) - m(\mathcal{M})$  independent of quark flavor (u,s,c,b) !

- need to first cancel the HF interaction contribution to meson masses:

$$\tilde{M}(V_i) = \frac{3M_{V_i} + M_{P_i}}{4}$$

- for spin-zero diquarks:

$$\begin{array}{cccccc} M(N) - \tilde{M}(\rho) & = & M(\Lambda) - \tilde{M}(K^*) & = & M(\Lambda_c) - \tilde{M}(D^*) & = & M(\Lambda_b) - \tilde{M}(B^*) \\ 323 \text{ MeV} & \approx & 321 \text{ MeV} & \approx & 312 \text{ MeV} & \approx & 310 \text{ MeV} \end{array}$$

- for spin-one diquarks need to also cancel HF contribution to baryon masses:

$$\tilde{M}(\Sigma_i) \equiv \frac{2M_{\Sigma_i^*} + M_{\Sigma_i}}{3}; \quad \tilde{M}(\Delta) \equiv \frac{2M_\Delta + M_N}{3}$$

$$\begin{array}{cccccc} \tilde{M}(\Delta) - \tilde{M}(\rho) & = & \tilde{M}(\Sigma) - \tilde{M}(K^*) & = & \tilde{M}(\Sigma_c) - \tilde{M}(D^*) & = & \tilde{M}(\Sigma_b) - \tilde{M}(B^*) \\ 617.56 \text{ MeV} & \approx & 526.43 \text{ MeV} & \approx & 523.95 \text{ MeV} & \approx & 512.45 \text{ MeV} \end{array}$$

## Magnetic moments of heavy baryons

- In  $\Lambda$ ,  $\Lambda_c$  and  $\Lambda_b$  light q coupled to spin zero
- $\rightarrow$  mag. moments determined by s,c,b moments
- quark mag. moments proportional to their chromomagnetic moments

$$\text{DGG: } \mu_\Lambda = -\frac{\mu_p}{3} \cdot \frac{M_{\Sigma^*} - M_\Sigma}{M_\Delta - M_N} = -0.61 \text{ n.m. } (= \text{EXP})$$

$\rightarrow$

$$\mu_{\Lambda_c} = -2\mu_\Lambda \cdot \frac{M_{\Sigma_c^*} - M_{\Sigma_c}}{M_{\Sigma^*} - M_\Sigma} = 0.43 \text{ n.m.}$$

$$\mu_{\Lambda_b} = \mu_\Lambda \cdot \frac{M_{\Sigma_b^*} - M_{\Sigma_b}}{M_{\Sigma^*} - M_\Sigma} = -0.067 \text{ n.m.}$$

challenge  
to EXP !

# Testing confining potentials through meson/baryon HF splitting ratio

B. Keren-Zur, hep-ph/0703011 & Ann. Phys

- from constituent quarks model can derive:

$$\frac{M_{K^*} - M_K}{M_{\Sigma^*} - M_\Sigma} = \frac{4}{3} \frac{\langle \psi | \delta(\vec{r}_u - \vec{r}_{\bar{s}}) | \psi \rangle_{meson}}{\langle \psi | \delta(\vec{r}_u - \vec{r}_s) | \psi \rangle_{baryon}}$$

- depends only on the confinement potential and quark mass ratio
- can be used to test different confinement potentials

# Testing confining potentials through meson/baryon HF splitting ratio

- 3 measurements ( $Q = s, c, b$ )
- 5 potentials:
  - Harmonic oscillator
  - Coulomb interaction
  - Linear potential
  - Linear + Coulomb
  - Logarithmic

# baryon/meson HF splitting ratio

- K meson HF splitting

$$M_{K^*} - M_K = 4v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_{\bar{s}})}{m_u m_s} \langle \psi | \delta(r_{us}) | \psi \rangle$$

- The  $\Sigma$  (uds) baryon HF splitting:

$$M_{\Sigma^*} - M_\Sigma = 6v_0 \frac{(\vec{\lambda}_u \cdot \vec{\lambda}_s)}{m_u m_s} \langle \psi | \delta(r_{us}) | \psi \rangle$$

- Using the relation:

$$(\vec{\lambda}_u \cdot \vec{\lambda}_s)_{meson} = 2(\vec{\lambda}_u \cdot \vec{\lambda}_s)_{baryon}$$

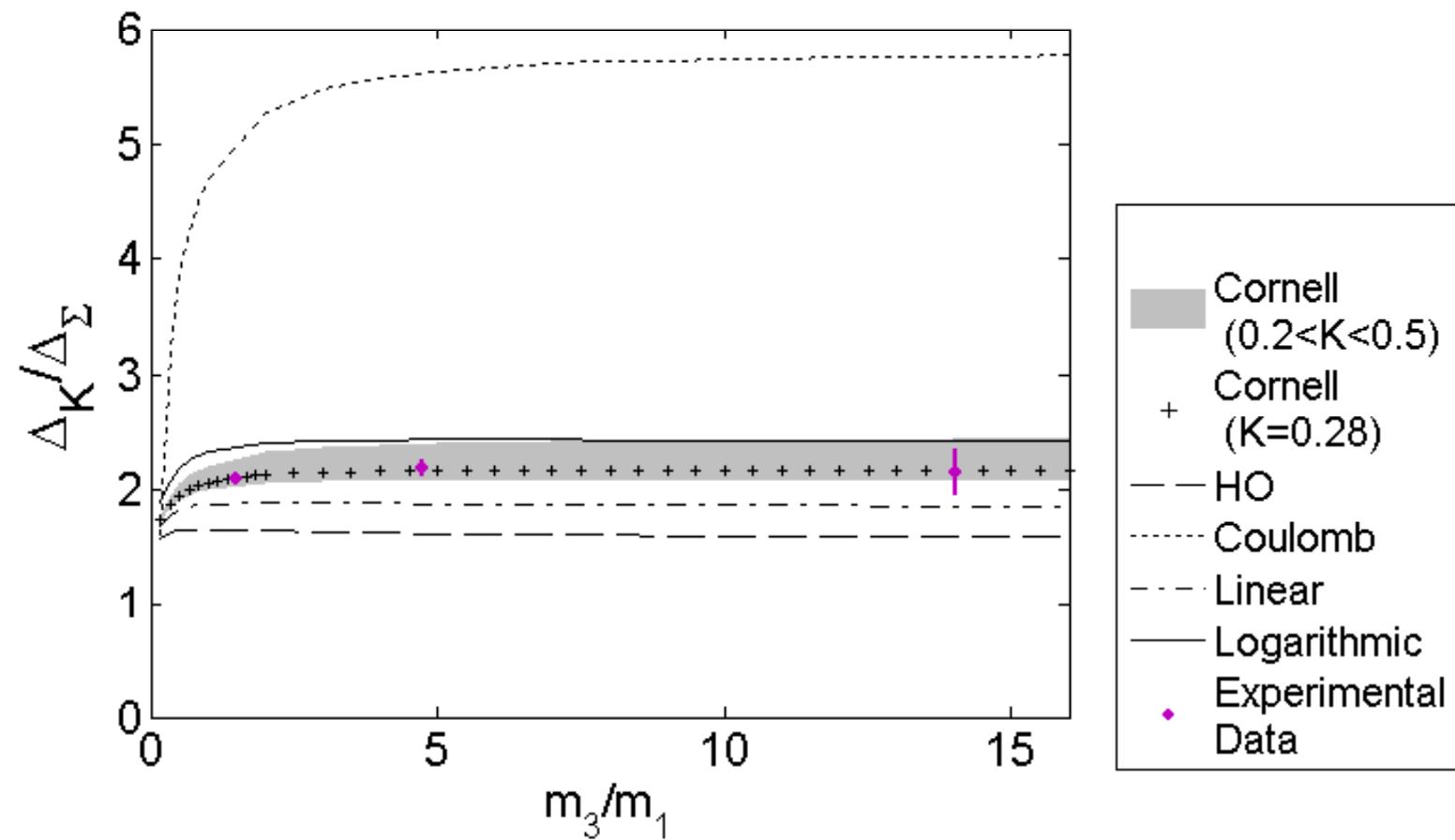
$$\boxed{\frac{M_{K^*} - M_K}{M_{\Sigma^*} - M_\Sigma} = \frac{4}{3} \frac{\langle \psi | \delta(r_{us}) | \psi \rangle_{meson}}{\langle \psi | \delta(r_{us}) | \psi \rangle_{baryon}}}$$

# baryon/meson HF splitting ratio

$$\frac{M_{K^*} - M_K}{M_{\Sigma^*} - M_\Sigma} = \frac{4}{3} \frac{\langle \psi | \delta(r_{us}) | \psi \rangle_{meson}}{\langle \psi | \delta(r_{us}) | \psi \rangle_{baryon}}$$

- similar quark content, so can cancel out the HF coupling constant ( $v_0$ ).
- confinement potential coupling constant and quark mass scale also cancel out
- depends only on the shape of the potential and the ratio of the quark masses.

# Hyperfine splitting ratio from potential models vs experiment



# hyperfine splitting ratio from potential models vs experiment

	$\Delta_K/\Delta_\Sigma$	$\Delta_D/\Delta_{\Sigma_c}$	$\Delta_B/\Delta_{\Sigma_b}$
$M_3/M_1$	1.33	4.75	14
EXP	$2.08 \pm 0.01$	$2.18 \pm 0.08$	$2.15 \pm 0.20$
Harmonic	1.65	1.62	1.59
Coulomb	$5.07 \pm 0.08$	$5.62 \pm 0.02$	$5.75 \pm 0.01$
Linear	$1.88 \pm 0.06$	$1.88 \pm 0.08$	$1.86 \pm 0.09$
Cornell (K=0.28)	$2.10 \pm 0.05$	$2.16 \pm 0.07$	$2.17 \pm 0.08$
Log	$2.38 \pm 0.02$	$2.43 \pm 0.02$	$2.43 \pm 0.01$

# Predicting the mass of $\Xi_Q$ baryons

$\Xi_Q$ : Qsd or Qsu. (sd), (sd) in spin-0

→  $\Xi_Q$  mass given by

$$\Xi_q = m_q + m_s + m_u - \frac{3v\langle\delta(r_{us})\rangle}{m_u m_s}$$

Can obtain (bsd) mass from (csd) + shift in HF:

$$\Xi_b = \Xi_c + (m_b - m_c) - \frac{3v}{m_u m_s} \left( \langle\delta(r_{us})\rangle_{\Xi_b} - \langle\delta(r_{us})\rangle_{\Xi_c} \right)$$

several options for obtaining  $m_b - m_c$  from data:

$$m_b - m_c = \Lambda_b - \Lambda_c = 3333.2 \pm 1.2 \text{ MeV}$$

$$m_b - m_c = \left( \frac{2\Sigma_b^* + \Sigma_b + \Lambda_b}{4} - \frac{2\Sigma_c^* + \Sigma_c + \Lambda_c}{4} \right) = 3330.4 \pm 1.8 \text{ MeV}$$

- The  $\Xi_Q^*(Qsq)$  baryons contain an s quark
- Q mass differences depend on the spectator
- optimal estimate from mesons which contain both s and Q:

$$m_b - m_c = \left( \frac{3B_s^* + B_s}{4} - \frac{3D_s^* + D_s}{4} \right) = 3324.6 \pm 1.4 \text{ MeV}$$

## Summary of $\Xi_b$ mass predictions

$m_b - m_c =$	$\Lambda_b - \Lambda_c$	$\Sigma_b - \Sigma_c$	$B_s - D_s$
	Eq. (6)	Eq. (7)	eq. (8)
No HF correction	$5803 \pm 2$	$5800 \pm 2$	$5794 \pm 2$
Linear	$5801 \pm 11$	$5798 \pm 11$	$5792 \pm 11$
Coulomb	$5778 \pm 2$	$5776 \pm 2$	$5770 \pm 2$
Cornell	$5799 \pm 7$	$5796 \pm 7$	$5790 \pm 7$

# Predictions for masses of $\Xi_b$ baryons

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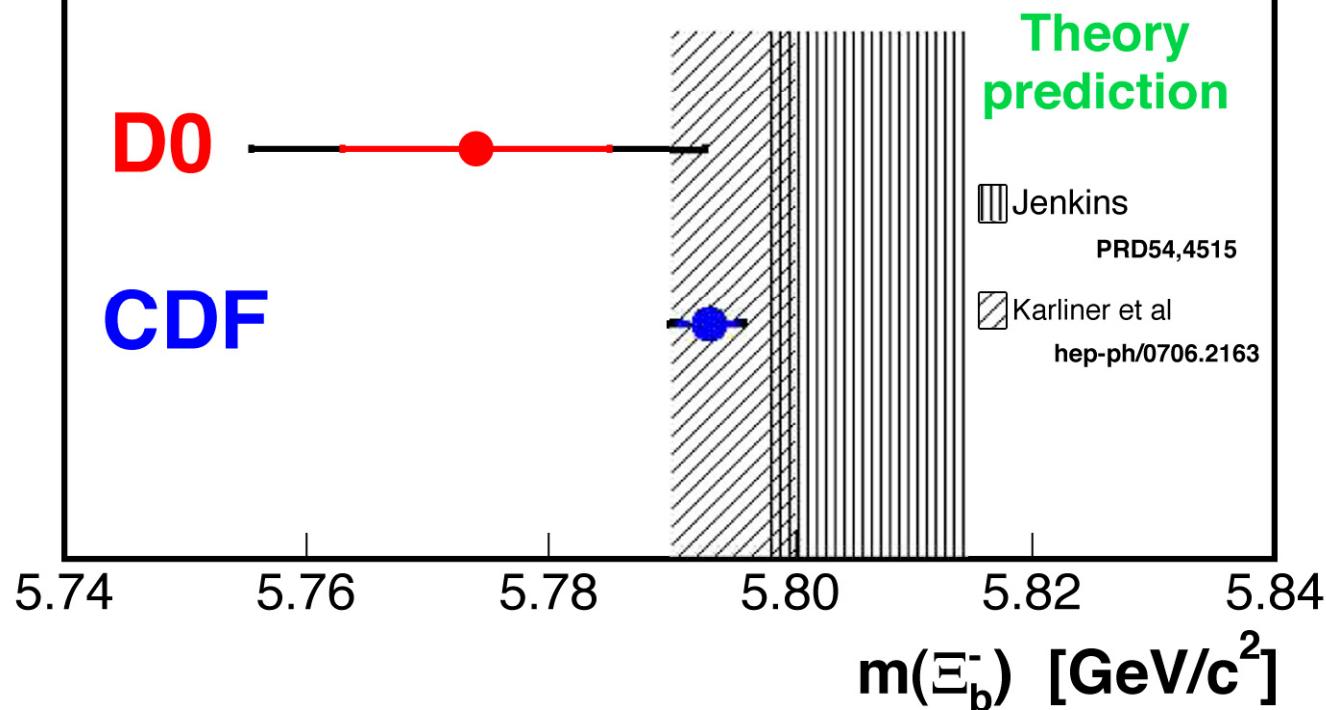
## ABSTRACT

The recent observation by CDF of  $\Sigma_b^\pm$  ( $uud$  and  $ddb$ ) baryons within 2 MeV of the predicted  $\Sigma_b - \Lambda_b$  splitting has provided strong confirmation for the theoretical approach based on modeling the color hyperfine interaction. We now apply this approach to predict the masses of the  $\Xi_b$  family of baryons with quark content  $usb$  and  $dsb$  – the ground state  $\Xi_b$  at 5790 to 5800 MeV, and the excited states  $\Xi'_b$  and  $\Xi^*_b$ . The main source of uncertainty is the method used to estimate the mass difference  $m_b - m_c$  from known hadrons. We verify that corrections due to the details of the interquark potential and to  $\Xi_b - \Xi'_b$  mixing are small.

**Observation and Mass Measurement of the Baryon  $\Xi_b^-$** 

(CDF Collaboration)

We report the observation and measurement of the mass of the bottom, strange baryon  $\Xi_b^-$  through the decay chain  $\Xi_b^- \rightarrow J/\psi \Xi^-$ , where  $J/\psi \rightarrow \mu^+ \mu^-$ ,  $\Xi^- \rightarrow \Lambda \pi^-$ , and  $\Lambda \rightarrow p \pi^-$ . A signal is observed whose probability of arising from a background fluctuation is  $6.6 \times 10^{-15}$ , or 7.7 Gaussian standard deviations. The  $\Xi_b^-$  mass is measured to be  $5792.9 \pm 2.5(\text{stat}) \pm 1.7(\text{syst}) \text{ MeV}/c^2$ .

$\Xi_b^-$  masses $\Xi_b^-$  Mass Comparison

30

## $\Xi_b^*$ , $\Xi'_b$ mass prediction

$\Xi'_b$  : bsd with (sd) in S=1; total spin = 1/2

$\Xi_b^*$  : bsd with (sd) in S=1; total spin = 3/2

spin-averaged mass of these two states

$$\frac{2\Xi_q^* + \Xi'_q}{3} = m_q + m_s + m_u + \frac{v \langle \delta(r_{us}) \rangle}{m_u m_s}$$

so that

$$\frac{2\Xi_b^* + \Xi'_b}{3} = \frac{2\Xi_c^* + \Xi'_c}{3} + (m_b - m_c) + \frac{2\Xi_c^* + \Xi'_c - 3\Xi_c}{12} \left( \frac{\langle \delta(r_{us}) \rangle_{\Xi_b}}{\langle \delta(r_{us}) \rangle_{\Xi_c}} - 1 \right)$$

## $\Xi_b^*$ , $\Xi'_b$ mass prediction

$$(2\Xi_b^* + \Xi'_b)/3$$


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	$m_b - m_c =$	$\Lambda_b - \Lambda_c$	$\Sigma_b - \Sigma_c$	$B_s - D_s$
	Eq. (6)	Eq. (7)	Eq. (8)	
No HF correction	$5956 \pm 3$	$5954 \pm 3$	$5948 \pm 3$	
Linear	$5957 \pm 4$	$5954 \pm 4$	$5948 \pm 4$	
Coulomb	$5965 \pm 3$	$5962 \pm 3$	$5956 \pm 3$	
Cornell	$5958 \pm 3$	$5955 \pm 3$	$5949 \pm 3$	

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difference between the spin averaged mass  
 $(2\Xi_b^* + \Xi'_b)/3$  and  $\Xi_b$  is roughly 150 – 160 MeV.

## $\Xi_b^*$ , $\Xi_b'$ mass prediction

- $\Xi_b^* - \Xi_b'$  mass difference more difficult to predict
- small due to the large  $m_b$ :  $\Xi_q^* - \Xi_q' = 3v \left( \frac{\langle \delta(r_{qs}) \rangle}{m_q m_s} + \frac{\langle \delta(r_{qu}) \rangle}{m_q m_u} \right)$

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$$\Xi_b^* - \Xi_b'$$

---

No HF correction  $24 \pm 2$

Linear  $28 \pm 6$

Coulomb  $36 \pm 7$

---

Cornell  $29 \pm 6$

---

using

$$\frac{m_s}{m_u} = 1.5 \pm 0.1, \frac{m_b}{m_c} = 2.95 \pm 0.2.$$

# Predictions for other bottom baryons

with B.Keren-Zur, H.J. Lipkin and J.L. Rosner

## $\Omega_b$ mass prediction

$$\begin{aligned}\frac{2\Omega_b^* + \Omega_b}{3} &= \frac{2\Omega_c^* + \Omega_c}{3} + (m_b - m_c) \\ &= \frac{2\Omega_c^* + \Omega_c}{3} + \frac{3B_s^* + B_s}{4} - \frac{3D_s^* + D_s}{4} \\ &= 6068.6 \pm 2.6 \text{ MeV}\end{aligned}$$

wavefunction correction  $\approx +2$  MeV.

HF splitting:  $m_b/m_c$  taken to be  $3.0 \pm 0.5$ .

$$\Omega_b^* - \Omega_b = (\Omega_c^* - \Omega_c) \frac{m_c}{m_b} = 23.6 \pm 4.0 \text{ MeV}$$

## $\Omega_b$ mass prediction

This gives the following mass predictions:

$$\Omega_b = 6052.1 \pm 5.6 \text{ MeV} \quad \Omega_b^* = 6082.8 \pm 5.6 \text{ MeV}$$

Wavefunction corrections give a factor of 1.28, and a splitting of  $30 \pm 6$  MeV.

Work in progress:

- $\Xi_b$  isospin splitting
- $\Lambda_b$  and  $\Xi_b$  orbital excitations
- $\Xi_{bc}$  (bcu)
- $\Xi_{cc}$  (ccu)

**Observation of the Doubly Strange  $b$  Baryon  $\Omega_b^-$** **D0 Collaboration**

We report the observation of the doubly strange  $b$  baryon  $\Omega_b^-$  in the decay channel  $\Omega_b^- \rightarrow J/\psi \Omega^-$ , with  $J/\psi \rightarrow \mu^+ \mu^-$  and  $\Omega^- \rightarrow \Lambda K^- \rightarrow (p\pi^-)K^-$ , in  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV. Using approximately  $1.3 \text{ fb}^{-1}$  of data collected with the D0 detector at the Fermilab Tevatron Collider, we observe  $17.8 \pm 4.9(\text{stat}) \pm 0.8(\text{syst}) \Omega_b^-$  signal events at a mass of  $6.165 \pm 0.010(\text{stat}) \pm 0.013(\text{syst}) \text{ GeV}$ . The significance of the observed signal is  $5.4\sigma$ , corresponding to a probability of  $6.7 \times 10^{-8}$  of it arising from a background fluctuation.

## $\Omega_b$ mass prediction

This gives the following mass predictions:

$$\Omega_b = 6052.1 \pm 5.6 \text{ MeV}$$

$$\Omega_b^* = 6082.8 \pm 5.6 \text{ MeV}$$

Wavefunction corrections give a factor of 1.28, and a splitting of  $30 \pm 6$  MeV.

Work in progress: "D0:  $\Omega_b=6165 +/- 10 \text{ (stat)} +/- 13 \text{ (syst.)}$   
either wrong or we don't understand something"  
M.K. @DIS'09

- $\Xi_b$  isospin splitting
- $\Lambda_b$  and  $\Xi_b$  orbital excitations
- $\Xi_{bc}$  (bcu)
- $\Xi_{cc}$  (ccu)

# Observation of the $\Omega_b^-$ Baryon and Measurement of the Properties of the $\Xi_b^-$ and $\Omega_b^-$ Baryons

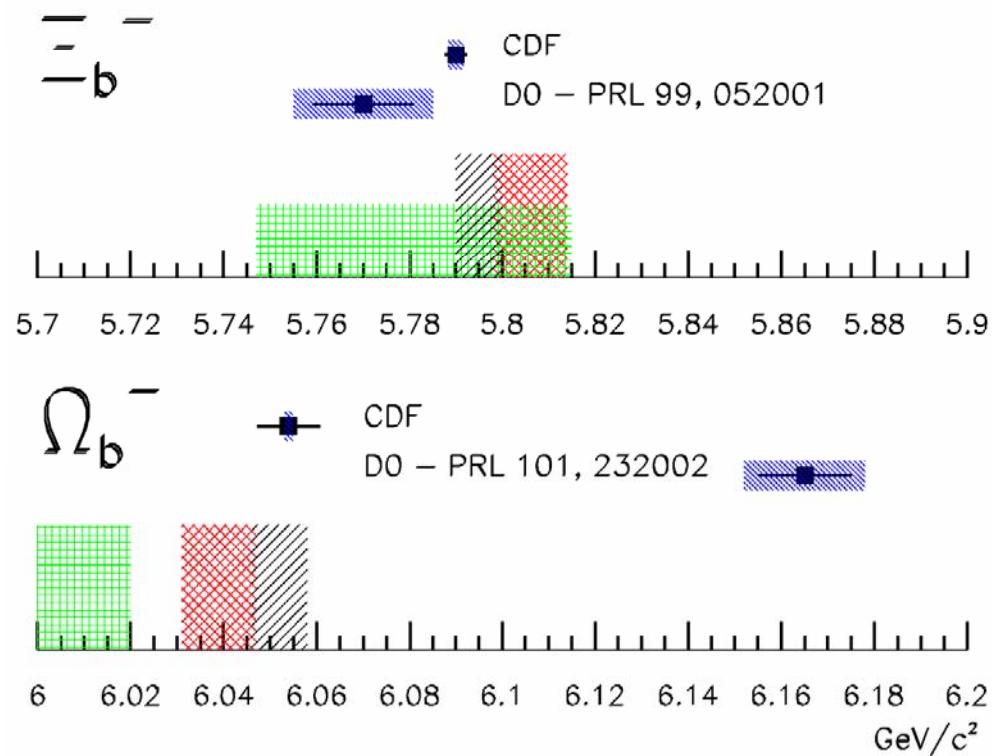
## CDF Collaboration

We report the observation of the bottom, doubly-strange baryon  $\Omega_b^-$  through the decay chain  $\Omega_b^- \rightarrow J/\psi \Omega^-$ , where  $J/\psi \rightarrow \mu^+ \mu^-$ ,  $\Omega^- \rightarrow \Lambda K^-$ , and  $\Lambda \rightarrow p \pi^-$ , using  $4.2 \text{ fb}^{-1}$  of data from  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96 \text{ TeV}$ , and recorded with the Collider Detector at Fermilab. A signal is observed whose probability of arising from a background fluctuation is  $4.0 \times 10^{-8}$ , or 5.5 Gaussian standard deviations. **The  $\Omega_b^-$  mass is measured to be  $6054.4 \pm 6.8(\text{stat.}) \pm 0.9(\text{syst.}) \text{ MeV}/c^2$ .** The lifetime of the  $\Omega_b^-$  baryon is measured to be  $1.13^{+0.53}_{-0.40}(\text{stat.}) \pm 0.02(\text{syst.}) \text{ ps}$ . In addition, for the  $\Xi_b^-$  baryon we measure a mass of  $5790.9 \pm 2.6(\text{stat.}) \pm 0.8(\text{syst.}) \text{ MeV}/c^2$  and a lifetime of  $1.56^{+0.27}_{-0.25}(\text{stat.}) \pm 0.02(\text{syst.}) \text{ ps}$ . Under the assumption that the  $\Xi_b^-$  and  $\Omega_b^-$  are produced with similar kinematic distributions to the  $\Lambda_b^0$  baryon, we find  $\frac{\sigma(\Xi_b^-) \mathcal{B}(\Xi_b^- \rightarrow J/\psi \Xi^-)}{\sigma(\Lambda_b^0) \mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda)} = 0.167^{+0.037}_{-0.025}(\text{stat.}) \pm 0.012(\text{syst.})$  and  $\frac{\sigma(\Omega_b^-) \mathcal{B}(\Omega_b^- \rightarrow J/\psi \Omega^-)}{\sigma(\Lambda_b^0) \mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda)} = 0.045^{+0.017}_{-0.012}(\text{stat.}) \pm 0.004(\text{syst.})$  for baryons produced with transverse momentum in the range of  $6 - 20 \text{ GeV}/c$ .



## Measured and Predicted Masses for the $\Xi_b^-$ and $\Omega_b^-$

- ██████ Jenkins (PRD 77,034012(2008))
- ████ Lewis et al, (PRD 79,014502(2009))
- █████ Karlíner et al, (Ann. Phys. 324,2(2008))
- █████ Systematic Uncertainties



## b–baryons spectrum – TH predictions vs EXP

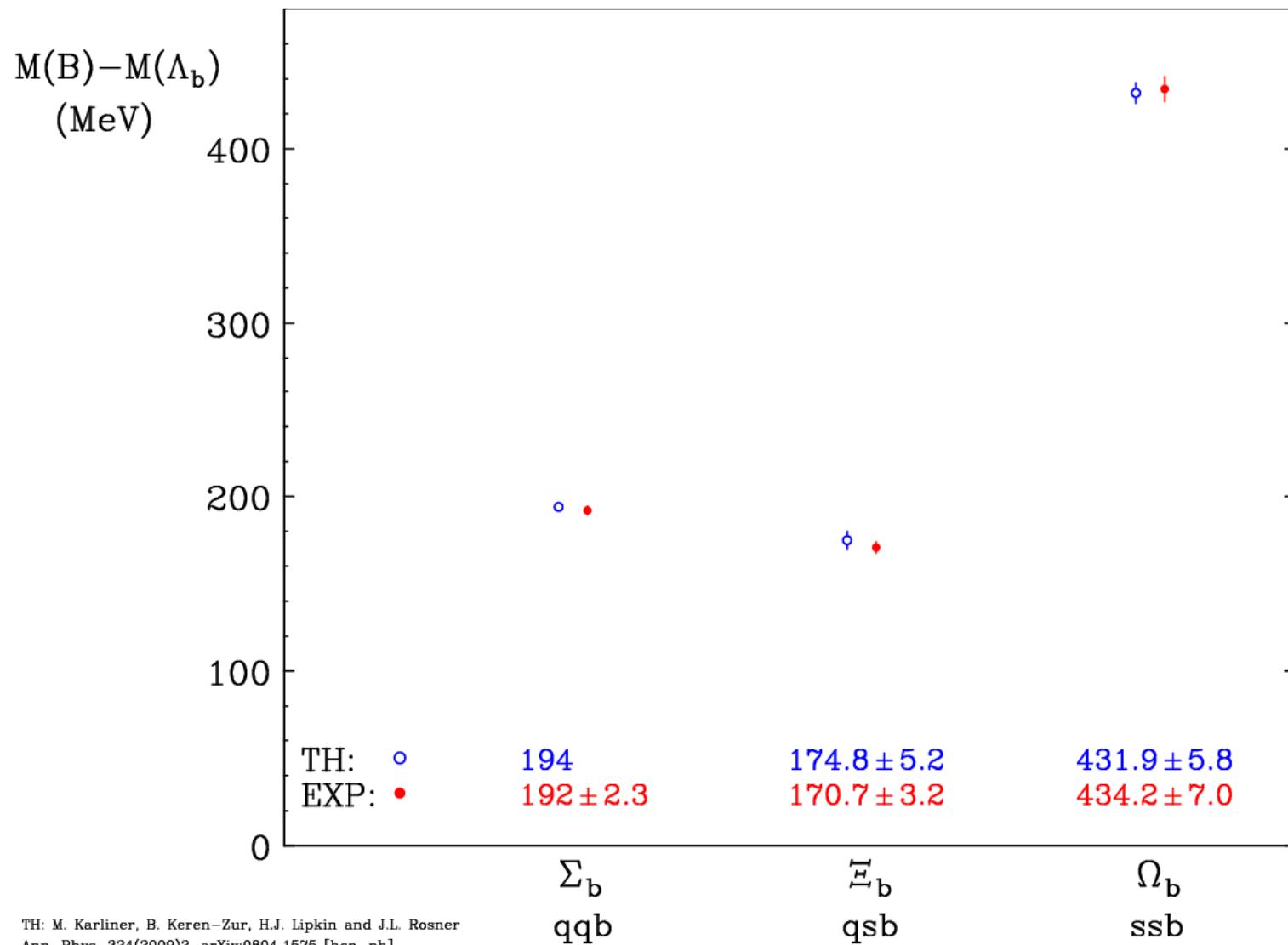


Table 10: Comparison of predictions for  $b$  baryons with those of some other recent approaches [6, 10, 11] and with experiment. Masses quoted are isospin averages unless otherwise noted. Our predictions are those based on the Cornell potential.

Quantity	Value in MeV				
	Refs. [6]	Ref. [10]	Ref. [11]	This work	Experiment
$M(\Lambda_b)$	5622	5612	Input	Input	$5619.7 \pm 1.7$
$M(\Sigma_b)$	5805	5833	Input	–	$5811.5 \pm 2$
$M(\Sigma_b^*)$	5834	5858	Input	–	$5832.7 \pm 2$
$M(\Sigma_b^*) - M(\Sigma_b)$	29	25	Input	$20.0 \pm 0.3$	$21.2_{-2.1}^{+2.2}$
$M(\Xi_b)$	5812	5806 <sup>a</sup>	Input	5790–5800	$5792.9 \pm 3.0^b$
$M(\Xi_b')$	5937	5970 <sup>a</sup>	$5929.7 \pm 4.4$	$5930 \pm 5$	–
$\Delta M(\Xi^b)^c$	–	–	–	$6.4 \pm 1.6$	–
$M(\Xi_b^*)$	5963	5980 <sup>a</sup>	$5950.3 \pm 4.2$	$5959 \pm 4$	–
$M(\Xi_b^*) - M(\Xi_b')$	26	10 <sup>a</sup>	$20.6 \pm 1.9$	$29 \pm 6$	–
$M(\Omega_b)$	6065	6081	$6039.1 \pm 8.3$	$6052.1 \pm 5.6$	–
$M(\Omega_b^*)$	6088	6102	$6058.9 \pm 8.1$	$6082.8 \pm 5.6$	–
$M(\Omega_b^*) - M(\Omega_b)$	23	21	$19.8 \pm 3.1$	$30.7 \pm 1.3$	–
$M(\Lambda_{b[1/2]}^*)$	5930	5939	–	$5929 \pm 2$	–
$M(\Lambda_{b[3/2]}^*)$	5947	5941	–	$5940 \pm 2$	–
$M(\Xi_{b[1/2]}^*)$	6119	6090	–	$6106 \pm 4$	–
$M(\Xi_{b[3/2]}^*)$	6130	6093	–	$6115 \pm 4$	–

<sup>a</sup>Value with configuration mixing taken into account; slightly higher without mixing.

<sup>b</sup>CDF [13] value of  $M(\Xi_b^-)$ .

<sup>c</sup> $M(\text{state with } d \text{ quark}) - M(\text{state with } u \text{ quark})$ .

Recent data from Belle:  
anomalously large (2 orders of mag.)

$$\Upsilon(5S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$$

$$\Upsilon(5S) \rightarrow \Upsilon(2S) \pi^+ \pi^-$$

0802.0649 [hep-ph], Lipkin & M.K.:  
might be mediated by  $\bar{b}b u \bar{d}$  tetraquark  
**below  $B\bar{B}$  threshold:**

$$\Upsilon(mS) \rightarrow T_{\bar{b}b}^\pm \pi^\mp \rightarrow \Upsilon(nS) \pi^+ \pi^-$$

analogous to Z(4430)? Seen in  $\psi' \pi^\pm$  but not in  $J/\psi \pi^\pm$

# Unique signal for $b\bar{b}q\bar{q}$ and $bbq$ double bottom baryons and $bb$ tetraquarks

- $b \rightarrow c\bar{c}s \rightarrow J/\psi s$

so  $bbq \rightarrow J/\psi J/\psi (ssq) \rightarrow J/\psi J/\psi \Xi$

similarly  $b\bar{b}q\bar{q} \rightarrow J/\psi J/\psi (s\bar{s}q\bar{q}) \rightarrow J/\psi J/\psi K\bar{K}$

and  $bb\bar{q}\bar{q}$

With all final state hadrons coming from the same vertex

Unique signature but v. low rate - is there enough data?

# Open questions

- need to understand the XYZ states in the charm sector and their counterparts in the bottom sector
- replacing charmed quark by bottom quark makes the binding stronger
- excellent challenge for EXP and TH
- general question of exotics in QCD
- **ccu, ccd** and **bbu, bbd**:  
SELEX ccq data - isospin breaking much too large?
- **$\eta_b$** : BaBar & CLEO.  $\Upsilon(1S)$  -  **$\eta_b$**  too large ?

## Summary

- Constituent quark model with color HF interaction gives highly accurate predictions for heavy baryon masses
- a challenge for theory: derivation from QCD
- constituent quark masses depend on the spectator quarks
- $M_{\Sigma_b} - M_{\Lambda_b} = 194 \text{ MeV}$  vs 192 in EXP (CDF)
- $M(\Sigma_b^*) - M(\Sigma_b) = 22 \text{ MeV}$  vs 21 MeV in EXP (CDF)
- $\mu_{\Lambda_c} = 0.43 \text{ n.m.}$     $\mu_{\Lambda_b} = -0.067 \text{ n.m.}$
- meson-baryon effective supersymmetry
- meson/baryon HF splitting confirms Cornell potential
- $\Xi_b, \Omega_b$  mass predictions: better than 3 MeV
- puzzle in Y(5S) decays:  $\bar{b}b u d \bar{d}$  candidates?

# Backup slides



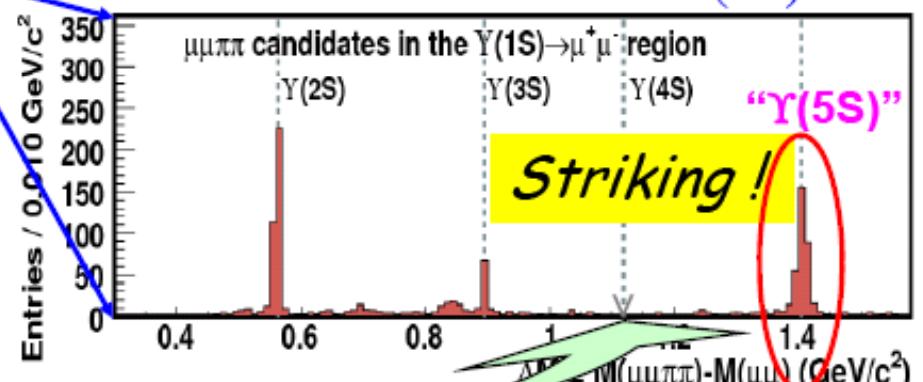
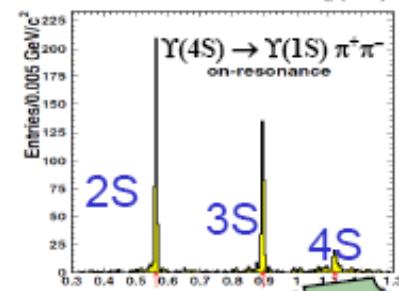
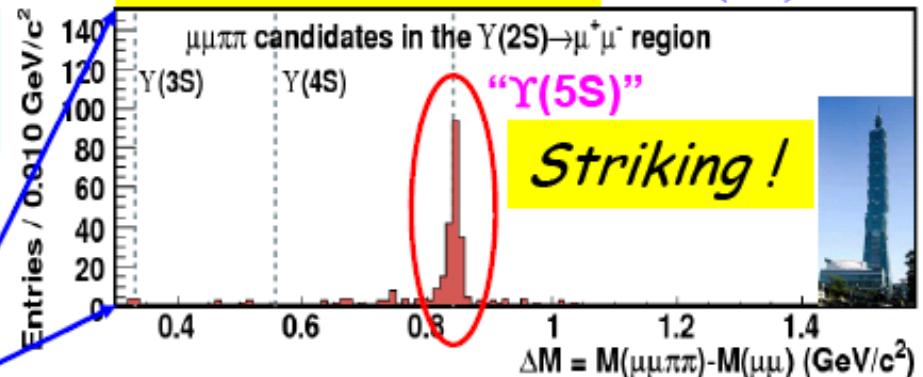
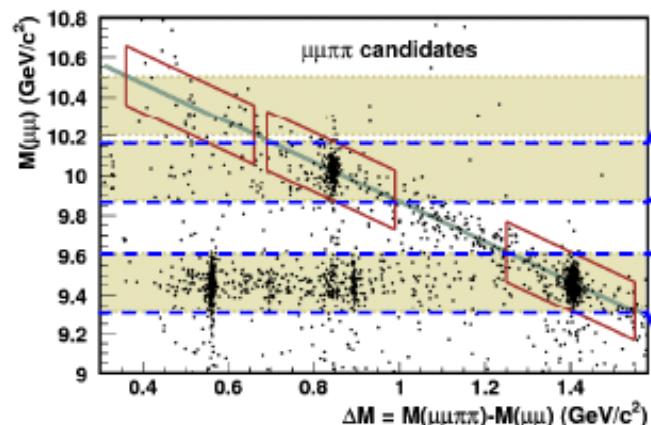
“ $\Upsilon(5S)$ ”  $\rightarrow \Upsilon(1S)\pi^+\pi^-$ ,  $\Upsilon(2S)\pi^+\pi^-$



“ $\Upsilon(5S)$ ”: single  $E_{CM}$  at 10.87 GeV  
Not clear whether  $\Upsilon(5S)$  itself.

expect  $O(1)$  events

$\Upsilon(2S)\pi^+\pi^-$



Expect to vanish

Hot Belle

George W.S. Hou (NTU)

FPCP08, 5/5/08 20



# Dalitz Plot: $Z^\pm(4430)$ Echoes? $c\bar{u}c\bar{d}$ ?



$\psi'\pi^\pm$

S.-K. Choi, S.L. Olsen et al., PRL '08

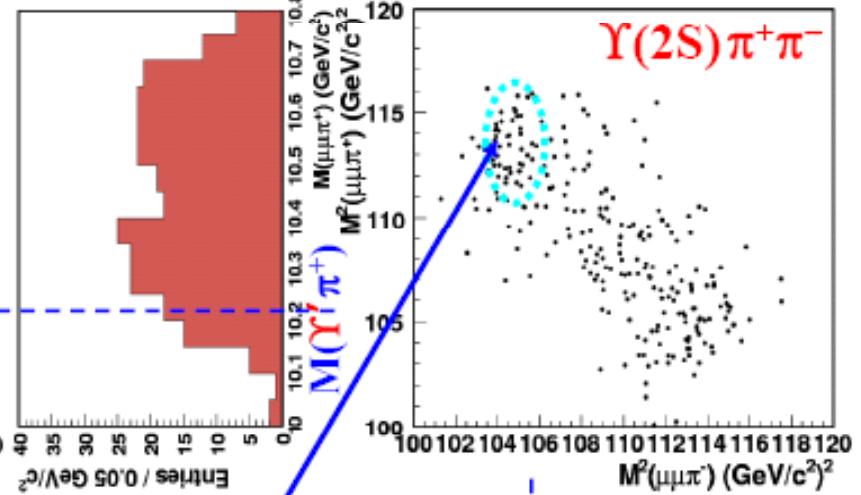
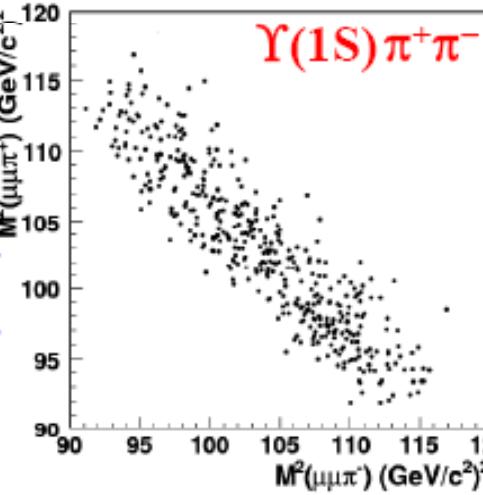
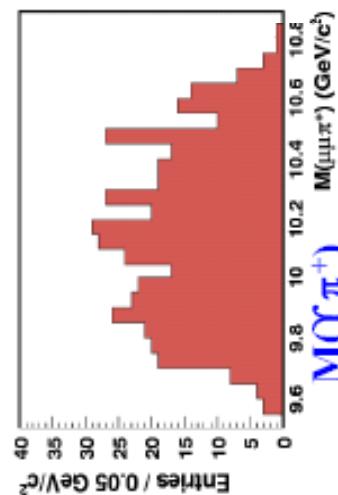


Karliner & Lipkin, arXiv:0802.0649 [hep-ph]

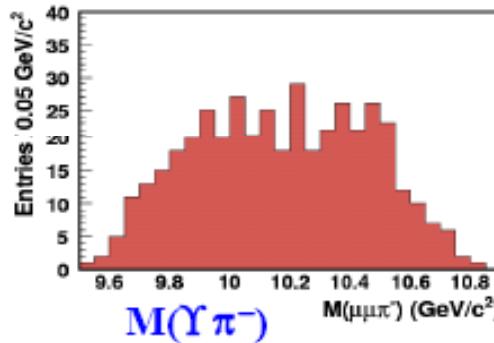
bub $\bar{d}$

Lighter than  $2m_B$ ?

cf. Cheung, Keung, Yuan, PRD '07: ~ 10700

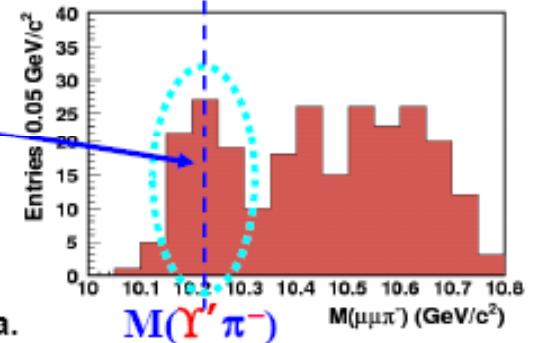


Nondescript



?

Too Early  
to Tell!  
Need more Data.



Hot Belle

George W.S. Hou (NTU)

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